

SCALE INVARIANT VOLKOV–AKULOV SUPERGRAVITY

S. FERRARA ^{a,b,c}, M. PORRATI ^{a,d} ¹ AND A. SAGNOTTI ^{a,e} ²^a *Th-Ph Department, CERN
CH - 1211 Geneva 23 SWITZERLAND*^b *INFN - Laboratori Nazionali di Frascati
Via Enrico Fermi 40, 00044 Frascati ITALY*^c *Department of Physics and Astronomy, University of California
Los Angeles, CA 90095-1547 USA*^d *CCPP, Department of Physics, NYU
4 Washington Pl., New York NY 10003, USA*^e *Scuola Normale Superiore and INFN
Piazza dei Cavalieri 7
56126 Pisa ITALY**sergio.ferrara@cern.ch, mp9@nyu.edu, sagnotti@sns.it*

ABSTRACT

A scale invariant Goldstino theory coupled to supergravity is obtained as a standard supergravity dual of a rigidly scale-invariant higher-curvature supergravity with a nilpotent chiral scalar curvature. The bosonic part of this theory describes a massless scalaron and a massive axion in a de Sitter Universe.

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1 Introduction

Motivated by single-field inflationary scenarios [1], several sgoldstinoless [2–5] supergravity extensions of inflationary models were recently considered [6–11] (for a recent review see [12]). Interestingly enough, in [7, 11] many of these models were linked to pure higher-derivative supergravity with a nilpotency constraint on the scalar curvature chiral superfield \mathcal{R} . These include the Volkov–Akulov–Starobinsky model [7] and the pure Volkov–Akulov theory coupled to supergravity [7]. Recently, the full component form of the latter theory was presented in [13, 14]

Along these lines, various authors considered R^2 theories of gravity [15] and their supergravity embeddings [15, 16], which possess a rigid scale invariance and naturally accommodate a de Sitter Universe. It is the aim of this note to give the sgoldstinoless version of these theories, which naturally combines an enhanced rigid scale invariance and a de Sitter geometry. This theory also emerges as a limiting case of the inflationary scenario.

2 Scale-Invariant Nilpotent Supergravity

The superspace action density of the scale-invariant theory that we consider ³,

$$\mathcal{A} = \frac{\mathcal{R}\overline{\mathcal{R}}}{g^2}\Big|_D + \sigma \mathcal{R}^2 S_0 \Big|_F, \quad (2.1)$$

where g is a dimensionless parameter, is invariant under the rigid scale transformations

$$\mathcal{R} \rightarrow \mathcal{R}, \quad S_0 \rightarrow e^{-\lambda} S_0, \quad \sigma \rightarrow e^{\lambda} \sigma. \quad (2.2)$$

This theory is equivalent to the theory considered in [16], supplemented with the nilpotency constraint

$$\mathcal{R}^2 = 0, \quad (2.3)$$

which is enforced by the chiral Lagrange multiplier σ present in the second term of eq. (2.1).

Using manipulations similar to those originally introduced in [17], we can now turn this model into a scale-invariant version of the Volkov–Akulov model coupled to standard supergravity. To this end, we first use the superspace identity

$$\sigma \mathcal{R}^2 S_0 + h.c. \Big|_F = \left(\sigma \frac{\mathcal{R}}{S_0} + \overline{\sigma} \frac{\overline{\mathcal{R}}}{\overline{S}_0} \right) S_0 \overline{S}_0 \Big|_D + \text{tot. deriv.}, \quad (2.4)$$

³We use throughout the conventions of [7].

and then introduce two Lagrange chiral superfield multipliers T and S according to

$$\mathcal{A} = \left(\sigma S + \bar{\sigma} \bar{S} + \frac{S \bar{S}}{g^2} \right) S_0 \bar{S}_0 \Big|_D - T \left(\frac{\mathcal{R}}{S_0} - S \right) S_0^3 + \text{h.c.} \Big|_F . \quad (2.5)$$

The final result is the standard supergravity action density

$$\mathcal{A} = - \left(T + \bar{T} - \sigma S - \bar{\sigma} \bar{S} - \frac{S \bar{S}}{g^2} \right) S_0 \bar{S}_0 \Big|_D + T S S_0^3 + \text{h.c.} \Big|_F + \text{tot. deriv.} \quad (2.6)$$

A final shift and a redefinition according to

$$T \rightarrow T + \sigma S , \quad X = \frac{S}{g} \quad (2.7)$$

yield the standard supergravity action density

$$\mathcal{A} = - (T + \bar{T} - X \bar{X}) S_0 \bar{S}_0 \Big|_D + W(T, X) S_0^3 + \text{h.c.} \Big|_F , \quad (2.8)$$

where

$$W(T, X, \sigma) = g T X + g^2 \sigma X^2 . \quad (2.9)$$

This is tantamount to the scale-invariant superpotential

$$W(T, X) = g T X , \quad (2.10)$$

where X is subject to the nilpotency constraint

$$X^2 = 0 , \quad (2.11)$$

so that X describes the sgoldstinoless Volkov–Akulov multiplet [2–5]. The corresponding bosonic Lagrangian,

$$\mathcal{L} = \frac{R}{2} - \frac{3}{(T + \bar{T})^2} |\partial T|^2 - g^2 \frac{|T|^2}{3(T + \bar{T})^2} , \quad (2.12)$$

is a special case of the result displayed in [7], so that it describes an $SU(1,1)/U(1)$ Kählerian model of curvature $-2/3$ with a scale-invariant positive potential. As a result, in terms of the canonical variable

$$T = e^{\phi \sqrt{\frac{2}{3}}} + i a \sqrt{\frac{2}{3}} , \quad (2.13)$$

one finds

$$\mathcal{L} = \frac{R}{2} - \frac{1}{2} (\partial \phi)^2 - \frac{1}{2} e^{-2\phi \sqrt{\frac{2}{3}}} (\partial a)^2 - \frac{g^2}{12} - \frac{g^2}{18} e^{-2\phi \sqrt{\frac{2}{3}}} a^2 . \quad (2.14)$$

Note that in the Einstein frame the metric is inert under the scale transformation corresponding to eq. (2.2), while

$$\phi \rightarrow \phi + \gamma , \quad a \rightarrow e^{\gamma \sqrt{\frac{2}{3}}} a . \quad (2.15)$$

3 de Sitter Vacuum Geometry

Since a is stabilized at zero, this model results in a de Sitter vacuum geometry, with a corresponding scale-invariant realization of supersymmetry breaking induced by the non-linear sgoldstinoless multiplet. The supersymmetry breaking scale M_s^2 is

$$M_s^2 = \frac{g}{2\sqrt{3}} M_{Planck}^2, \quad (3.1)$$

up to a conventional numerical factor. Eq. (2.8) describes the minimal supergravity model that embodies a scale-invariant goldstino interaction and leads unavoidably to a de Sitter geometry. This model involves a single dimensionless parameter g , which determines its *positive* vacuum energy according to

$$V = \frac{g^2}{12} M_{Planck}^4. \quad (3.2)$$

In contrast, the Volkov–Akulov model coupled to supergravity, depends on the two parameters f and W_0 , and consequently leads to a vacuum energy [18] [19] [20] [7] [13]

$$V = \frac{1}{3} |f|^2 - 3 |W_0|^2 \quad (3.3)$$

of arbitrary sign.

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References

- [1] A. A. Starobinsky, “A New Type of Isotropic Cosmological Models Without Singularity,” Phys. Lett. **B 91** (1980) 99; D. Kazanas, “Dynamics of the Universe and Spontaneous Symmetry Breaking,” Astrophys. J. **241** (1980) L59; K. Sato, “Cosmological Baryon Number Domain Structure and the First Order Phase Transition of a Vacuum,” Phys. Lett. B **99** (1981) 66; A. H. Guth, “The Inflationary Universe: A Possible Solution to the Horizon and Flatness Problems,” Phys. Rev. **D 23** (1981) 347; V. F. Mukhanov and G. V. Chibisov, “Quantum Fluctuation and Nonsingular Universe. (In Russian),” JETP Lett. **33** (1981) 532 [Pisma Zh.

- Eksp. Teor. Fiz. **33** (1981) 549]; A. D. Linde, “A New Inflationary Universe Scenario: A Possible Solution of the Horizon, Flatness, Homogeneity, Isotropy and Primordial Monopole Problems,” Phys. Lett. **B 108** (1982) 389; A. Albrecht and P. J. Steinhardt, “Cosmology for Grand Unified Theories with Radiatively Induced Symmetry Breaking,” Phys. Rev. Lett. **48** (1982) 1220; A. D. Linde, “Chaotic Inflation,” Phys. Lett. **B129** (1983) 177; For recent reviews see: N. Bartolo, E. Komatsu, S. Matarrese and A. Riotto, “Non-Gaussianity from inflation: Theory and observations,” Phys. Rept. **402** (2004) 103 [astro-ph/0406398]; V. Mukhanov, “Physical foundations of cosmology,” Cambridge, UK: Univ. Pr. (2005); S. Weinberg, “Cosmology,” Oxford, UK: Oxford Univ. Pr. (2008); D. H. Lyth and A. R. Liddle, “The primordial density perturbation: Cosmology, inflation and the origin of structure,” Cambridge, UK: Cambridge Univ. Pr. (2009); D. S. Gorbunov and V. A. Rubakov, “Introduction to the theory of the early Universe: Cosmological perturbations and inflationary theory,”; J. Martin, C. Ringeval and V. Vennin, “Encyclopaedia Inflationaris,” arXiv:1303.3787 [astro-ph.CO].
- [2] D. V. Volkov and V. P. Akulov, “Is the Neutrino a Goldstone Particle?,” Phys. Lett. B **46** (1973) 109.
- [3] M. Rocek, “Linearizing the Volkov-Akulov Model,” Phys. Rev. Lett. **41** (1978) 451; U. Lindstrom and M. Rocek, “Constrained Local Superfields,” Phys. Rev. D **19** (1979) 2300.
- [4] R. Casalbuoni, S. De Curtis, D. Dominici, F. Feruglio and R. Gatto, “Nonlinear Realization of Supersymmetry Algebra From Supersymmetric Constraint,” Phys. Lett. B **220** (1989) 569.
- [5] Z. Komargodski and N. Seiberg, “From Linear SUSY to Constrained Superfields,” JHEP **0909** (2009) 066 [arXiv:0907.2441 [hep-th]], “Comments on Supercurrent Multiplets, Supersymmetric Field Theories and Supergravity,” JHEP **1007** (2010) 017 [arXiv:1002.2228 [hep-th]].
- [6] L. Alvarez-Gaume, C. Gomez and R. Jimenez, “Minimal Inflation,” Phys. Lett. B **690** (2010) 68 [arXiv:1001.0010 [hep-th]], “A Minimal Inflation Scenario,” JCAP **1103** (2011) 027 [arXiv:1101.4948 [hep-th]].
- [7] I. Antoniadis, E. Dudas, S. Ferrara and A. Sagnotti, “The Volkov-Akulov-Starobinsky Supergravity,” Phys. Lett. B **733** (2014) 32 [arXiv:1403.3269 [hep-th]];

- [8] S. Ferrara, R. Kallosh and A. Linde, “Cosmology with Nilpotent Superfields,” JHEP **1410** (2014) 143 [arXiv:1408.4096 [hep-th]];
- [9] R. Kallosh and A. Linde, “Inflation and Uplifting with Nilpotent Superfields,” JCAP **1501** (2015) 01, 025 [arXiv:1408.5950 [hep-th]];
- [10] G. Dall’Agata and F. Zwirner, “On sgoldstino-less Supergravity models of inflation,” JHEP **1412** (2014) 172 [arXiv:1411.2605 [hep-th]].
- [11] E. Dudas, S. Ferrara, A. Kehagias and A. Sagnotti, “Properties of Nilpotent Supergravity,” arXiv:1507.07842 [hep-th].
- [12] S. Ferrara and A. Sagnotti, “Some Pathways in non-Linear Supersymmetry: Special Geometry Born-Infeld’s, Cosmology and dualities,” arXiv:1506.05730 [hep-th], to appear in a special issue of “p-Adic Numbers, Ultrametric Analysis and Applications” devoted to Prof. V. .S. Varadarajan.
- [13] E. A. Bergshoeff, D. Z. Freedman, R. Kallosh and A. Van Proeyen, “Pure de Sitter Supergravity,” arXiv:1507.08264 [hep-th].
- [14] F. Hasegawa and Y. Yamada, “Component action of nilpotent multiplet coupled to matter in 4 dimensional $\mathcal{N} = 1$ supergravity,” arXiv:1507.08619 [hep-th].
- [15] C. Kounnas, D. Lst and N. Toumbas, “ R^2 inflation from scale invariant supergravity and anomaly free superstrings with fluxes,” Fortsch. Phys. **63** (2015) 12 [arXiv:1409.7076 [hep-th]]; L. Alvarez-Gaume, A. Kehagias, C. Kounnas, D. Lust and A. Riotto, “Aspects of Quadratic Gravity,” arXiv:1505.07657 [hep-th].
- [16] S. Ferrara, A. Kehagias and M. Porrati, “ \mathcal{R}^2 Supergravity,” JHEP **1508** (2015) 001 [arXiv:1506.01566 [hep-th]].
- [17] S. Cecotti, “Higher Derivative Supergravity Is Equivalent To Standard Supergravity Coupled To Matter. 1.,” Phys. Lett. B **190** (1987) 86.
- [18] D. Z. Freedman, P. van Nieuwenhuizen and S. Ferrara, “Progress Toward a Theory of Supergravity,” Phys. Rev. D **13** (1976) 3214; S. Deser and B. Zumino, “Consistent Supergravity,” Phys. Lett. B **62** (1976) 335. For a review see: D. Z. Freedman and A. Van Proeyen, “Supergravity,” (Cambridge Univ. Press, 2012).

- [19] S. Deser and B. Zumino, “Broken Supersymmetry and Supergravity,” *Phys. Rev. Lett.* **38** (1977) 1433.
- [20] E. Cremmer, B. Julia, J. Scherk, P. van Nieuwenhuizen, S. Ferrara and L. Girardello, “Superhiggs effect in Supergravity with general scalar interactions,” *Phys. Lett. B* **79** (1978) 231, “Spontaneous Symmetry Breaking and Higgs Effect in Supergravity Without Cosmological Constant,” *Nucl. Phys. B* **147** (1979) 105; E. Cremmer, S. Ferrara, L. Girardello and A. Van Proeyen, “Coupling Supersymmetric Yang-Mills Theories to Supergravity,” *Phys. Lett. B* **116** (1982) 231, “Yang-Mills Theories with Local Supersymmetry: Lagrangian, Transformation Laws and SuperHiggs Effect,” *Nucl. Phys. B* **212** (1983) 413.